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## KURT GÖDEL RESEARCH CENTER FOR MATHEMATICAL LOGIC

### UNIVERSITÄT WIEN

## 1090 WIEN, WÄHRINGER STRASSE 25

#### O.UNIV.-PROF. DR. SY-DAVID FRIEDMAN

#### INVITATION

## STEFAN HOFFELNER (KGRC)

# $\mathbf{NS}_{\omega_1}$ SATURATED AND A $\Sigma_4^1\text{-}\mathbf{DEFINABLE}$ WELLORDER ON THE REALS

#### Abstract:

The investigation of the saturation of the nonstationary ideal  $NS_{\omega_1}$  has a long tradition in set theory. In the early 1970's K. Kunen showed that, given a huge cardinal, there is a universe in which  $NS_{\omega_1}$  is  $\aleph_2$ -saturated. The assumption of a huge cardinal has been improved in the following decades, using very different techniques, by many set theorists until S. Shelah around 1985 realized that already a Woodin cardinal is sufficient for the consistency of the statement " $NS_{\omega_1}$  is saturated".

Due to work of H. Woodin on the one hand and G. Hjorth on the other, there is a surprising and deep connection between definable wellorders of the reals and the saturation of  $NS_{\omega_1}$ : In a universe with a measurable cardinal and  $NS_{\omega_1}$  saturated, it is impossible to have a  $\Sigma_3^1$ -wellorder. This leads naturally to the question whether there is a universe in which  $NS_{\omega_1}$  is saturated and its reals have a  $\Sigma_4^1$ -wellorder. In my talk I will outline a proof that this is indeed the case; assuming the existence of  $M_1^{\#}$  there is a model with a  $\Sigma_4^1$ -definable wellorder on the reals in which  $NS_{\omega_1}$  is saturated.

This is joint work with Sy-David Friedman.



THURSDAY, MAY 11, 2017 Tea at 3:30pm in the KGRC meeting room (room 104) Talk at 4:00pm in the KGRC lecture room (room 101) GÖDEL RESEARCH CENTER JOSEPHINUM, 1090 WIEN, WÄHRINGER STRASSE 25

o.Univ.-Prof. Dr. Sy-David Friedman